

Where Are We Now?

Real-Time Estimates of the Macro Economy

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1 Aim

- To describe a method for calculating daily real-time estimates of the current state of the U.S. economy.
- The method needs to allow for:
 - variable reporting lags,
 - temporal aggregation,
 - missing data.
- This paper focuses on the problem of estimating the current level of and growth rate in GDP.
- The method can be applied to any (macro) variable of interest.

2 Why Real-Time Estimates are Needed

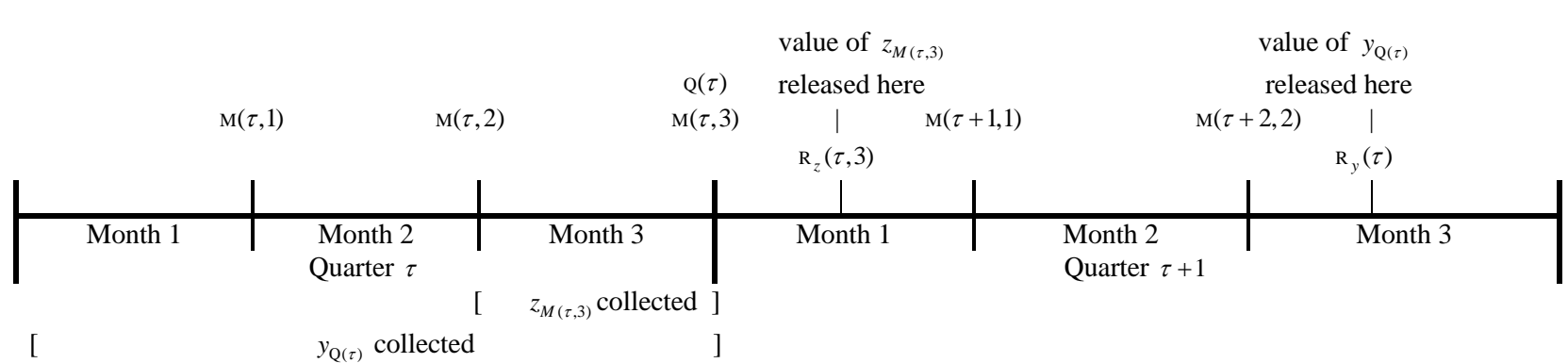
- Policy-making:
 - Information on real economic activity is collected by government agencies, but
 - the collection, aggregation and dissemination process takes time. \Rightarrow
 - data releases represent official aggregations of past rather than current economic activity.
- Asset Pricing:
 - Information about the current state of real economic activity is widely dispersed across consumers, firms and policy-makers.
 - Individuals are unaware of the contemporaneous consumption, saving, investment and employment decisions made by others.
 - This lack of timely information can significantly alter the dynamics of asset prices (Evans and Lyons 2004).

3 Real-Time Estimates and Real Time Data

- Real-Time Data: Croushore and Stark (1999, 2001), Orphanides (2001) and others
 - A set of *historical* values for a variable that are known on a particular date.
 - Represents a *subset* of public information available on a particular date.
- Real-Time Estimates:
 - An estimate of the current value of GDP (growth) based on public information available at the time.
 - I use an information set that spans the history of data releases on GDP and 18 other macroeconomic variables.
 - Additional variables (e.g. asset prices) can easily be added.

4 Earlier Work

- Clarida, Kitchen and Monaco (2002):
 - Regression-based method
- Features of this method:
 - Estimates come from a single fully-specified econometric model.
 - A wide variety of variables can be computed from the estimated model.
 - * The model can provide real-time forecasts for GDP growth for *any* future quarter.
 - We can construct high frequency estimates of real-economic activity.



GDP Announcements

The BEA releases GDP data for quarter τ as:

- “advanced” growth
- “preliminary” growth
- “final” growth
- (annual revisions that generally lead to revisions in the “final” data values released over the previous three years).

$$y_{r(\tau)} = \Delta^q x_{q(\tau)} + v_{r(\tau)}, \quad (1)$$

where

- $x_{q(\tau)}$ = log of real GDP for quarter τ ($\Delta^q x_{q(\tau)} \equiv x_{q(\tau)} - x_{q(\tau-1)}$)
- $y_{r(\tau)}$ = “final” data released on day $r_y(\tau)$
- $r_y(\tau) - q(\tau)$ = the reporting lag for quarterly data.

“Final” GDP:

$$y_{r(\tau)} = E \left[\Delta^q x_{q(\tau)} | \Omega_{q(\tau)} \right] + E \left[v_{r(\tau)} | \Omega_{q(\tau)} \right] + \left(y_{r(\tau)} - E \left[y_{r(\tau)} | \Omega_{q(\tau)} \right] \right). \quad (2)$$

The noise term can be decomposed as

$$y_{r(\tau)} - E \left[y_{r(\tau)} | \Omega_{q(\tau)} \right] = \left(E \left[y_{r(\tau)} | \Omega_{q(\tau)}^{\text{bea}} \right] - E \left[y_{r(\tau)} | \Omega_{q(\tau)} \right] \right) + \left(y_{r(\tau)} - E \left[y_{r(\tau)} | \Omega_{q(\tau)}^{\text{bea}} \right] \right), \quad (3)$$

“Advanced” and “Preliminary” GDP:

$$\hat{y}_{r(\tau)} = y_{r(\tau)} + \tilde{e}_{r(\tau)} + \hat{e}_{r(\tau)}, \quad (4)$$

$$\tilde{y}_{r(\tau)} = y_{r(\tau)} + \tilde{e}_{r(\tau)}, \quad (5)$$

The Inference Problem

Decompose quarterly GDP growth into a sequence of daily increments:

$$\Delta^q x_{q(\tau)} = \sum_{i=1}^{d(\tau)} \Delta x_{q(\tau-1)+i}, \quad (6)$$

where $d(\tau) \equiv q(\tau) - q(\tau - 1)$.

Next, project $z_{r(\tau,j)}^i$ on a portion of GDP growth

$$z_{r(\tau,j)}^i = \beta_i \Delta^m x_{m(\tau,j)} + u_{m(\tau,j)}^i, \quad (7)$$

where $\Delta^m x_{m(\tau,j)}$ is the contribution to GDP growth in quarter τ during month j :

$$\Delta^m x_{m(\tau,j)} \equiv \sum_{i=m(\tau,j-1)+1}^{m(\tau,j)} \Delta x_i.$$

Real-Time Estimates of GDP

The real-time estimates are based on the 3 GDP releases and 18 monthly macro series; $z^i = 1, 2, \dots, 18$:

$$E[\Delta^q x_{q(\tau)} | \Omega_{q(\tau)}], \quad (8)$$

where

$$\begin{aligned} \Omega_t &= \Omega_t^z \cup \Omega_t^y \\ \Omega_t^y &\equiv \{ \hat{y}_{r(\tau)}, \tilde{y}_{r(\tau)}, y_{r(\tau)} : r(\tau) < t \} \\ \Omega_t^z &\equiv \bigcup_{i=1}^{21} \left\{ z_{r(\tau, j)}^i : r(\tau, j) < t \text{ for } j = 1, 2, 3 \right\} \end{aligned}$$

We can also compute *daily* real-time estimates of quarterly GDP, and GDP growth:

$$x_{q(\tau)|i} \equiv E[x_{q(\tau)} | \Omega_i] \quad (9)$$

$$\Delta^q x_{q(\tau)|i} \equiv E[\Delta^q x_{q(\tau)} | \Omega_i]. \quad (10)$$

for $q(\tau - 1) < i \leq q(\tau)$.

7 The Model

Define the partial sums

$$s_t^q \equiv \sum_{i=q(\tau)+1}^{\min\{q(\tau),t\}} \Delta x_i, \quad s_t^m \equiv \sum_{i=m(\tau,j-1)+1}^{\min\{m(\tau,j),t\}} \Delta x_i$$

Let

$$\lambda_t^m = \begin{cases} 1 & \text{if } t = m(\tau, j) + 1, \text{ for } j = 1, 2, 3, \\ 0 & \text{otherwise,} \end{cases}$$
$$\lambda_t^q = \begin{cases} 1 & \text{if } t = q(\tau) + 1, \\ 0 & \text{otherwise.} \end{cases}$$

so

$$s_t^q = (1 - \lambda_t^q) s_{t-1}^q + \Delta x_t, \tag{11}$$

$$s_t^m = (1 - \lambda_t^m) s_{t-1}^m + \Delta x_t. \tag{12}$$

Quarterly GDP growth one and two quarters back are

$$\Delta^{q(1)}x_t = (1 - \lambda_t^q) \Delta^{q(1)}x_{t-1} + \lambda_t^q s_{t-1}^q. \quad (13)$$

$$\Delta^{q(2)}x_t = (1 - \lambda_t^q) \Delta^{q(2)}x_t + \lambda_t^q \Delta^{q(1)}x_{t-1}. \quad (14)$$

- If t is the first day of a new quarter, $\lambda_t^q = 1, \Rightarrow \Delta^{q(1)}x_{q(\tau)+1} = s_{q(t)}^q = \Delta^q x_{q(\tau)}$
- On all other days, $\Delta^{q(1)}x_t = \Delta^{q(1)}x_{t-1}$.

When the reporting lag for “final” GDP is one quarter

$$y_t = \Delta^{q(1)}x_t + v_{r(\tau)}, \quad (15)$$

and when the lag is two quarters,

$$y_t = \Delta^{q(2)}x_t + v_{r(\tau)}. \quad (16)$$

The contribution GDP growth in the last (completed) month is given by

$$\Delta^{m(1)}x_t = (1 - \lambda_t^m) \Delta^{m(1)}x_{t-1} + \lambda_t^m s_{t-1}^m, \quad (17)$$

and the contribution from i (> 1) months back is

$$\Delta^{m(i)}x_t = (1 - \lambda_t^m) \Delta^{m(i)}x_t + \lambda_t^m \Delta^{m(i-1)}x_{t-1}. \quad (18)$$

If the reporting lag for macro series i is less than one month, the value released on day t can be written as

$$z_t^i = \beta_i \Delta^{m(1)}x_t + u_t^i. \quad (19)$$

In cases where the reporting lag is two months,

$$z_t^i = \beta_i \Delta^{m(2)}x_t + u_t^i. \quad (20)$$

If the series ($i = 18$) is released *before* the end of the month in which the survey data are collected

$$z_t^{18} = \beta_{18} s_t^m + u_t^{18}. \quad (21)$$

To complete the model we need to specify the dynamics for the daily contributions, Δx_t .

$$\Delta x_t = \sum_{i=1}^k \phi_i \Delta^{m(i)} x_t + e_t, \quad (22)$$

- The daily contribution on day t only depends on the history of Δx_t insofar as it is summarized by the monthly contributions, $\Delta^{m(i)} x_t$.
- The process aggregates up to a $\text{AR}(k)$ process for $\Delta^m x_{m(\tau,j)}$ at the monthly frequency.

8 Estimation

Problems:

1. There is a pure inference problem of how to compute $E[x_{q(\tau)}|\Omega_i]$ and $E[\Delta^q x_{q(\tau)}|\Omega_i]$
2. We need to estimate the model parameters from the three data releases on GDP and the 18 other macro series.
 - the individual data releases are irregularly spaced, and
 - arrive in a non-synchronized manner.

Solution: Write the model in State Space Form and Estimate with the Kalman Filter

In the case where Δx_t depend only on last month's contribution, the state equation is

$$\begin{bmatrix} s_t^Q \\ \Delta^{Q(1)}x_t \\ \Delta^{Q(2)}x_t \\ s_t^M \\ \Delta^{M(1)}x_t \\ \Delta^{M(2)}x_t \\ \Delta x_t \end{bmatrix} = \begin{bmatrix} 1 - \lambda_t^Q & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ \lambda_t^Q & 1 - \lambda_t^Q & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & \lambda_t^Q & 1 - \lambda_t^Q & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 - \lambda_t^M & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & \lambda_t^M & 1 - \lambda_t^M & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & \lambda_t^M & 1 - \lambda_t^M & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & \phi_1 & 0 & 0 \end{bmatrix} \begin{bmatrix} s_{t-1}^Q \\ \Delta^{Q(1)}x_{t-1} \\ \Delta^{Q(2)}x_{t-1} \\ s_{t-1}^M \\ \Delta^{M(1)}x_{t-1} \\ \Delta^{M(2)}x_{t-1} \\ \Delta x_{t-1} \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ e_t \end{bmatrix},$$

or, more compactly

$$\mathbb{Z}_t = \mathbb{A}_t \mathbb{Z}_{t-1} + \mathbb{V}_t.$$

The link between the data releases and elements of the state vector is described by

$$\begin{bmatrix} \hat{y}_t \\ \tilde{y}_t \\ y_t \\ z_t^1 \\ \vdots \\ z_t^{18} \end{bmatrix} = \begin{bmatrix} 0 & \text{QL}_t^1(\hat{y}) & \text{QL}_t^2(\hat{y}) & 0 & 0 & 0 & 0 \\ 0 & \text{QL}_t^1(\tilde{y}) & \text{QL}_t^2(\tilde{y}) & 0 & 0 & 0 & 0 \\ 0 & \text{QL}_t^1(y) & \text{QL}_t^2(y) & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \beta_1 \text{ML}_t^0(z^1) & \beta_i \text{ML}_t^1(z^1) & \beta_1 \text{ML}_t^2(z^1) & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ 0 & 0 & 0 & \beta_{18} \text{ML}_t^0(z^{18}) & \beta_{18} \text{ML}_t^1(z^{18}) & \beta_{18} \text{ML}_t^2(z^{18}) & 0 \end{bmatrix} \mathbf{Z}_t + \begin{bmatrix} \hat{e}_t + \tilde{e}_t + v_t \\ \tilde{e}_t + v_t \\ v_t \\ u_t^1 \\ \vdots \\ u_t^{18} \end{bmatrix},$$

or

$$\mathbf{X}_t = \mathbf{C}_t \mathbf{Z}_t + \mathbf{U}_t.$$

$\text{QL}_t^i(\varkappa) = 1$ when the reporting lag for series \varkappa lies between $i - 1$ and i quarters, and zero otherwise.

$\text{ML}_t^i(\varkappa)$ is the monthly version of $\text{QL}_t^i(\varkappa)$

Table 1: Data Series (4/11/93 - 6/30/99)

	Release	Obs.	Reporting Lag
Quarterly	Advanced GDP	26	1-2 Months
	Preliminary GDP	25	2-3 Months
	Final GDP	26	3-4 Months
Monthly			
Real Activity	Nonfarm Payroll Employment	78	3 - 9 days
	Retail Sales	78	12-15 days
	Industrial Production	78	15-18 days
	Capacity Utilization	78	15-18 days
	Personal Income	76	30-33 days
	Consumer Credit	78	33-40 days
Consumption	Personal Consumption Expenditures	76	30-33 days
	New Home Sales	77	27-33 days
Investment	Durable Goods Orders	77	24-29 days
	Construction Spending	77	31-34 days
	Factory Orders	76	29-35 days
	Business Inventories	78	38-44 days
Government	Government Budget Deficit	78	15-21 days
Net Exports	Trade Balance	78	44-53 days
Forward-looking	Consumer Confidence Index	78	-8-0 days
	NAPM index	78	0-6 days
	Housing Starts	77	14-20 days
	Index of Leading Indicators	78	27-45 days
Distribution of Data Releases			
Releases per Day	Fraction of Sample	Observations	
0	45.48%	765	
1	38.76%	652	
2	10.46%	176	
3	4.34%	73	
4	0.95%	16	
> 0	54.52%	917	

Table 2: Model Estimates

A: Process for Δx_t		ϕ_1	ϕ_2	ϕ_3	ϕ_4	ϕ_5	ϕ_6	σ_e
estimate**		-0.384	0.296	0.266	-0.289	-0.485	0.160	3.800
standard error**		(0.004)	(0.003)	(0.003)	(0.003)	(0.003)	(0.004)	(0.010)
B: Quarterly Data Releases		ω_i	sdt(ω_i)*					
$i = a$	Advanced GDP Growth	0.508	(0.177)					
p	Preliminary GDP Growth	1.212	(0.312)					
C: Monthly Data Releases		α_i	sdt(α_i)*	β_i	sdt(β_i)*	σ_i	sdt(σ_i)*	
$i = 1$	Nonfarm Payroll Employment	0.007	(0.218)	0.656	(0.301)	0.932	(0.171)	
2	Retail Sales	-0.047	(0.282)	0.285	(0.136)	0.381	(0.082)	
3	Industrial Production	-0.028	(0.145)	0.189	(0.090)	0.229	(0.035)	
4	Capacity Utilization	0.924	(0.088)	0.125	(0.114)	0.382	(0.020)	
5	Personal Income	-0.291	(0.219)	0.038	(0.126)	0.227	(0.040)	
6	Consumer Credit	0.389	(0.300)	-0.160	(0.966)	2.961	(0.494)	
7	Personal Consumption Expenditures	-0.405	(0.206)	0.133	(0.074)	0.111	(0.029)	
8	New Home Sales	0.726	(0.170)	-0.011	(0.171)	0.473	(0.071)	
9	Durable Goods Orders	-0.224	(0.258)	0.989	(0.753)	1.999	(0.413)	
10	Construction Spending	0.312	(0.197)	-0.135	(0.233)	0.655	(0.123)	
11	Factory Orders	-0.194	(0.288)	0.997	(0.489)	-0.856	(0.306)	
12	Business Inventories	0.128	(0.277)	-0.019	(0.061)	0.228	(0.032)	
13	Government Budget Deficit	-0.359	(0.418)	-0.992	(1.423)	3.262	(0.508)	
14	Trade Balance	0.819	(0.189)	0.361	(0.602)	1.585	(0.344)	
15	Consumer Confidence Index	0.977	(0.076)	0.208	(0.136)	-0.482	(0.084)	
16	NAPM index	0.849	(0.115)	-0.008	(0.047)	0.151	(0.024)	
17	Housing Starts	0.832	(0.175)	0.002	(0.026)	0.071	(0.014)	
18	Index of Leading Indicators	0.107	(0.240)	0.212	(0.077)	0.231	(0.033)	

Notes: "*" and "**" indicate that the reported estimate or standard error is multiplied by 100 and 25 respectively.

Table 3: Model Diagnostics

Innovation Autocorrelations		ρ_1	BPQ(1)	ρ_6	BPQ (6)
Quarterly Releases					
	Advanced GDP	0.058	(0.766)	-0.061	(0.889)
	Preliminary GDP	-0.364	(0.069)	-0.034	(0.012)
	Final GDP	0.001	(0.996)	-0.172	(0.729)
Monthly Releases					
$i = 1$	Nonfarm Payroll Employment	-0.023	(0.841)	0.051	(0.902)
2	Retail Sales	0.005	(0.966)	-0.028	(0.789)
3	Industrial Production	0.005	(0.963)	0.003	(0.981)
4	Capacity Utilization	-0.029	(0.800)	0.147	(0.885)
5	Personal Income	-0.069	(0.687)	0.057	(0.770)
6	Consumer Credit	-0.091	(0.422)	0.310	(0.040)
7	Personal Consumption Expenditures	0.122	(0.477)	-0.021	(0.427)
8	New Home Sales	-0.219	(0.084)	-0.056	(0.220)
9	Durable Goods Orders	-0.094	(0.418)	-0.121	(0.650)
10	Construction Spending	0.064	(0.699)	0.131	(0.798)
11	Factory Orders	-0.161	(0.327)	-0.113	(0.483)
12	Business Inventories	-0.068	(0.552)	0.339	(0.000)
13	Government Budget Deficit	-0.091	(0.421)	-0.137	(0.100)
14	Trade Balance	-0.203	(0.077)	0.087	(0.578)
15	Consumer Confidence Index	0.047	(0.678)	-0.111	(0.624)
16	NAPM index	-0.067	(0.556)	-0.017	(0.639)
17	Housing Starts	-0.160	(0.161)	-0.127	(0.518)
18	Index of Leading Indicators	0.021	(0.850)	0.043	(0.525)

Notes: ρ_i denotes the sample autocorrelation at lag i . p-values are calculated for the null hypothesis of $\rho_i = 0$.

Table 4: Forecast Comparisons

A:	Data Revision		Model	
	Mean	M.S.E.	Mean	M.S.E.
Advanced	0.246	(0.446)	0.090	(0.441)
Preliminary	0.038	(0.067)	0.040	(0.066)
Combined	0.142	(0.257)	0.065	(0.254)
B:	M.M.S.		Model	
	Mean	M.S.E.	Mean	M.S.E.
In-sample				
Advanced	0.729	(1.310)	0.190	(1.407)
Preliminary	0.160	(0.249)	0.096	(0.418)
Final	0.042	(0.062)	0.080	(0.395)
Combined	0.310	(0.540)	0.122	(0.740)
Out-of-sample				
Advanced	0.985	(1.464)	0.380	(1.500)
Preliminary	0.046	(0.178)	0.178	(0.801)
Final	-0.015	(0.057)	0.099	(0.208)
Combined	0.338	(0.566)	0.219	(0.836)

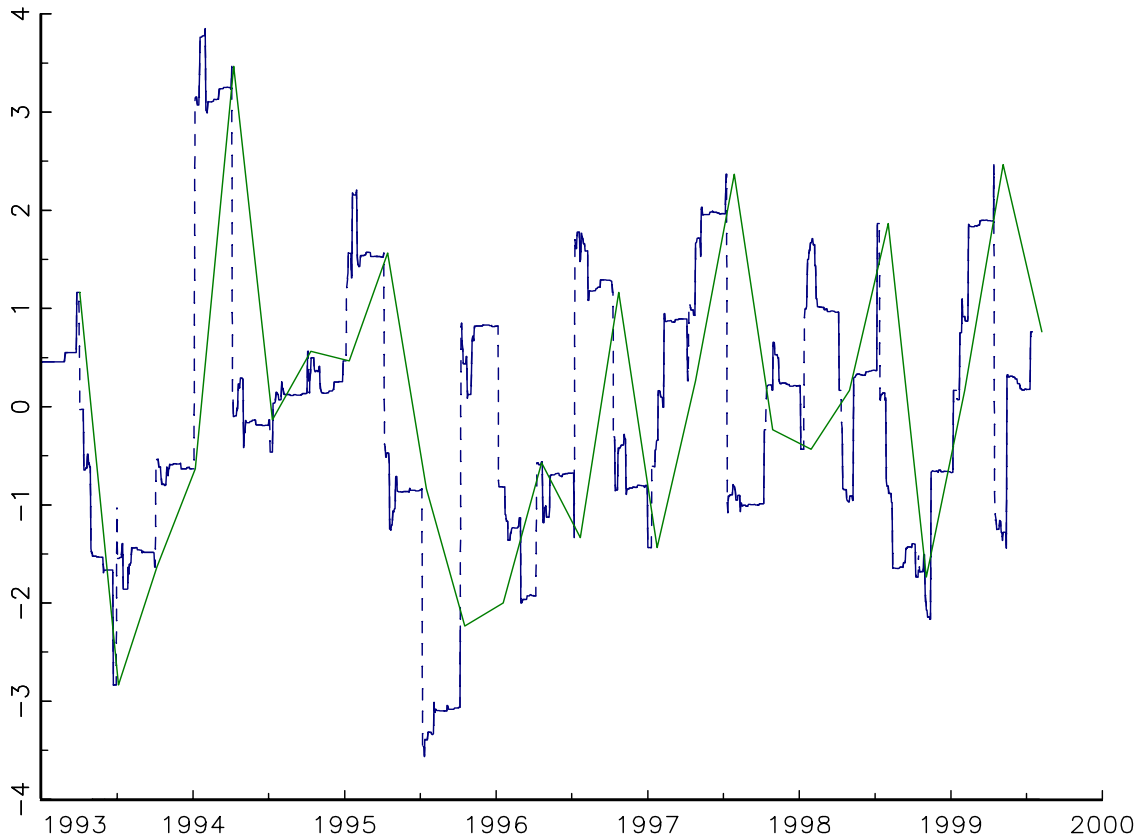


Figure 2: Real-time estimates of quarterly GDP growth $\Delta^Q x_{Q(\tau)|t}$ where $Q(\tau) < t \leq R_y(\tau)$ (blue line), and “final” releases for GDP growth (green line).

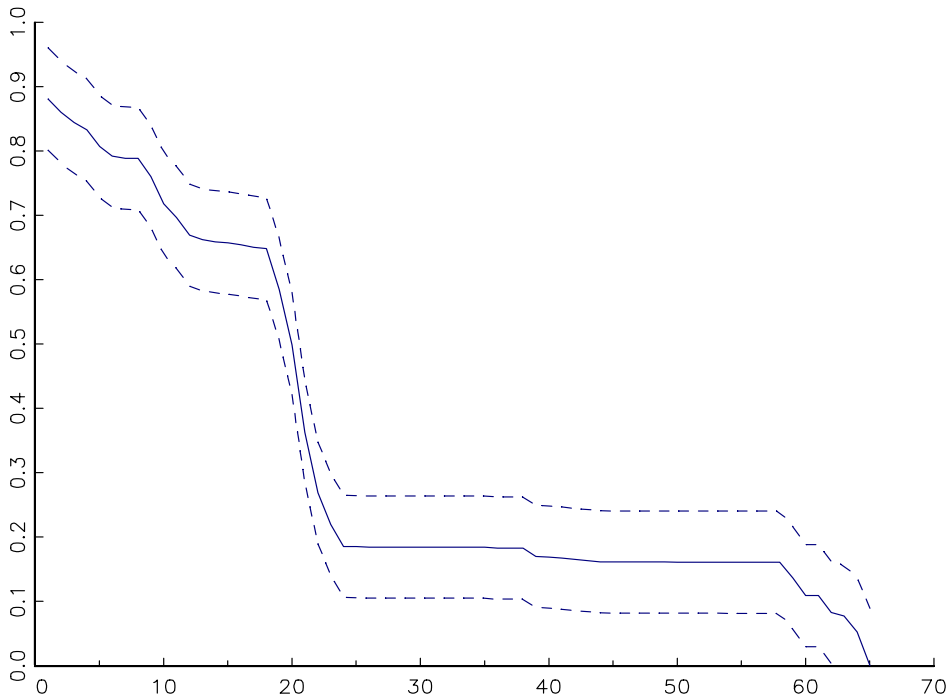


Figure 3: The solid line is the sample average of $\mathbb{V}(\Delta^Q x_{Q(\tau)} | \Omega_{Q(\tau)+i})$ for $0 < i \leq R_y(\tau) - Q(\tau)$, and the dashed lines denote the 95% confident band. The horizontal axis marks the the number of days i past the end of quarter $Q(\tau)$.

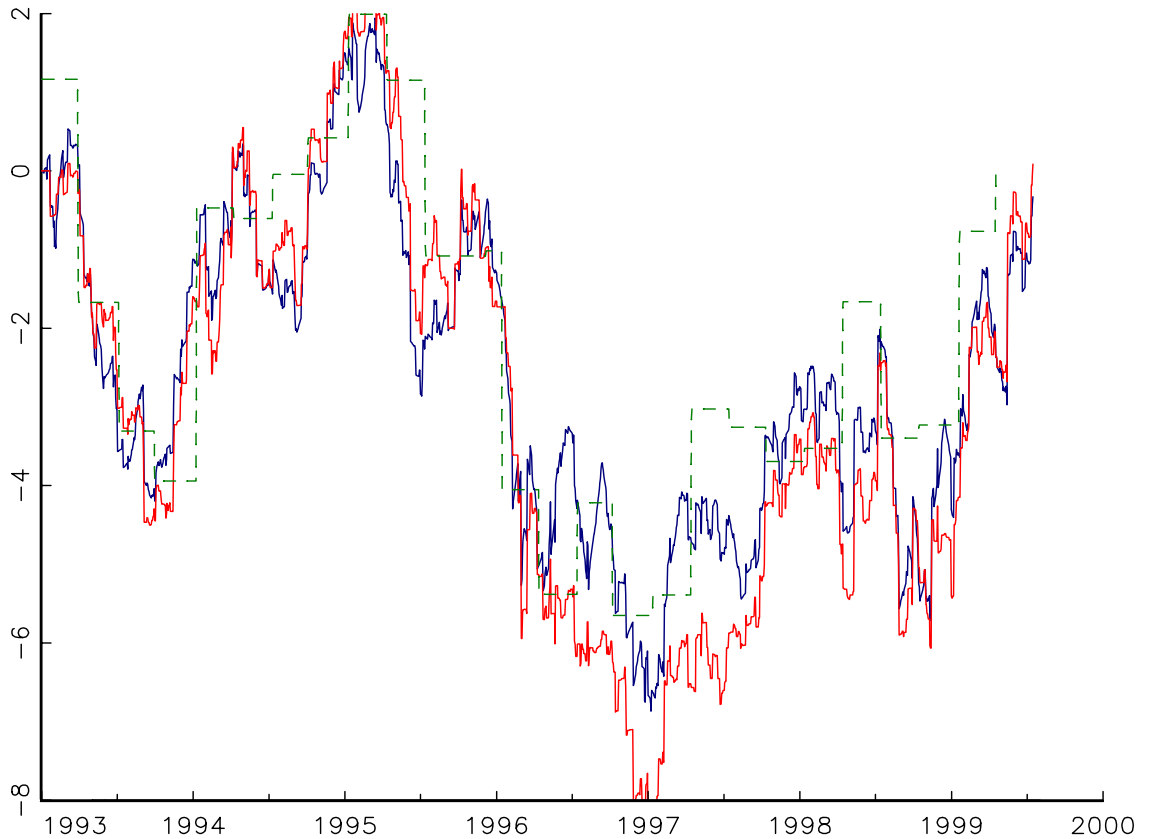


Figure 4: Real-time estimates of log GDP $x_{Q(\tau)|t}$ (red line), $E[x_t|\Omega_t]$ (blue line) and cumulant of “final” GDP releases (green dashed line).

$$x_{Q(\tau)|t} = \mathbb{E}[x_t|\Omega_t] + \sum_{h=1}^{Q(\tau)-t} \mathbb{E}[\Delta x_{t+h}|\Omega_t].$$

Table 5: Monthly Indicator Estimates

	Data Release	a_i	std(a_i)	b_i	std(b_i)	R^2
$i = 1$	Nonfarm Payroll Employment	0.224*	(0.033)	0.330*	(0.050)	0.233
2	Retail Sales	0.520*	(0.074)	0.838*	(0.099)	0.186
3	Industrial Production	0.745*	(0.116)	1.047*	(0.142)	0.233
4	Capacity Utilization	-0.006	(0.034)	0.066	(0.057)	0.010
5	Personal Income	-0.110	(0.132)	0.163	(0.224)	0.003
6	Consumer Credit	0.001	(0.012)	-0.002	(0.019)	0.000
7	Personal Consumption Expenditures	0.377*	(0.182)	0.603*	(0.277)	0.033
8	New Home Sales	0.016	(0.069)	0.181*	(0.088)	0.039
9	Durable Goods Orders	0.013	(0.021)	0.064*	(0.027)	0.030
10	Construction Spending	-0.050	(0.051)	-0.102	(0.060)	0.015
11	Factory Orders	0.097*	(0.038)	0.160*	(0.043)	0.066
12	Business Inventories	-0.013	(0.152)	0.289	(0.247)	0.008
13	Government Budget Deficit	-0.008	(0.011)	-0.017	(0.016)	0.005
14	Trade Balance	-0.071*	(0.021)	-0.068*	(0.030)	0.042
15	Consumer Confidence Index	0.068*	(0.028)	0.060	(0.037)	0.021
16	NAPM index	-0.001	(0.145)	0.514*	(0.216)	0.046
17	Housing Starts	-1.330*	(0.421)	0.705	(0.546)	0.012
18	Index of Leading Indicators	0.164	(0.179)	0.476*	(0.199)	0.038

Notes: The table reports the OLS estimates of a_i and b_i from equations (??) and (??). Both equations are estimated at the daily frequency, and the standard errors are corrected for the MA(19) process induced by the overlapping data. The right hand column reports the R^2 statistic from estimating equation (??). A “*” denotes significance at the 5 per cent level.

9 Conclusion

Results

- the estimates of log GDP display a good deal of high-frequency volatility.
- the gaps between the real-time estimates and ex post GDP data are on occasion both persistent and significant.
- monthly data releases contain information that is useful for forecasting its future path of GDP.
- standard proxies for real activity at the monthly frequency capture only a fraction of the variance in the real-time estimates

Topics for the Future

- Can real-time estimates and forecasts to identify turning points in the business cycle?
- Can real-time estimates bring a new perspective to the link between asset prices and macroeconomic fundamentals? Evans and Lyons (2004a).